

Optical Properties of Blown and Cast Polyethylene Films: Surface Versus Bulk Structural Considerations

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ABSTRACT: In this article we report on some surprising, and we believe new, findings regarding the factors affecting the optical properties (haze) of polyethylene blown and cast films. A comprehensive investigation of blown and cast films made from conventional Ziegler-Natta catalyzed linear low density polyethylene (LLDPE) as well as metallocene-catalyzed LLDPE (mLLDPE) resins was conducted. The large majority of the contribution to the total haze in the blown and cast films was observed to come from the surface roughness of the films, with the bulk (internal) contribution being relatively minor. Using a variety of analysis and characterization methods, including atomic force microscopy, small angle light scattering, and wide angle X-ray scattering, we determined that the surface roughness in these films was a result of the development of distinct spherulitic-like superstructures formed during the blown or cast film processing. Furthermore, these superstructures were observed only in the mLLDPE blown films, and not in the LLDPE blown films processed at similar conditions. Analysis of the rheological and molecular characteristics of these various mLLDPE and LLDPE resins revealed that the mLLDPE resins exhibited considerably lower molecular weight, narrower molecular weight distribution, lower zero shear viscosity, and lower melt elasticity compared with the LLDPE resins of similar melt index. These observations support our general finding and primary conclusion from this work that in polyethylene blown and cast films made using typical processing conditions, the optical haze properties are adversely affected because of enhanced surface roughness caused by the formation of spherulitic-like superstructures in polymer melts that possess fast relaxing and low melt elasticity rheological characteristics. © 2000 John Wiley & Sons, Inc. *J Appl Polym Sci* 77: 2845–2864, 2000

INTRODUCTION

The market for polyethylene film is enormous and is continually growing with a major component of that market being packaging. The optical properties of films (such as haze, transparency or clarity, and transmittance) are key issues in packaging

applications, because they allow the consumer to “see” what is contained within the package. Hence, the optical properties are important features in the marketability of a particular product and control of these properties is therefore required whether the film is used for food packaging, pallet wrap, or other related applications.

The terms clarity, haze, turbidity, transparency, etc. are often used interchangeably, and sometimes without distinction, to describe the optical properties of a product. However, it is impor-

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tant to realize that these various terms and measures are different and can, on some occasions, point in opposite directions. In this work, we have focused primarily on the haze measurement as a proxy for the optical properties. Furthermore, because haze and clarity are generally observed to be inversely dependent, i.e., high haze yields low (poor) clarity and vice-versa, we use these two terms interchangeably.

In the case of polyethylene blown films, haze is affected by light scattering and reflection/refraction because of both bulk and surface roughness effects. Previous publications¹⁻⁴ have mentioned a loss of film clarity arising from bulk scattering and/or surface irregularities that also promote turbidity because of surface effects. Such publications have rightly noted that bulk scattering can arise from a number of sources including voids or any other internal structural fluctuations that promote changes in refractive index on the scale of the wavelength of light (400–700 nm), which are responsible for turbidity enhancement. In fact, there have been numerous fundamental studies on the light-scattering characterization of semicrystalline films of polyethylene as well as other polymers whereby the superstructure effects that promote this turbidity are well quantified.⁵⁻¹⁰ For example, in the case of spherulitic superstructure, a morphology common to polymers crystallized without deformation, the general theoretical relations indicate that the scattering by such structures roughly scales with the sixth power of the radius¹¹ and thereby indicate that, other factors being equal, a smaller size superstructure will lead to higher clarity relative to a comparable anisotropic larger-scale body. As a result, this particular point has distinctly been recognized in the cases of many products such as molded bottles, etc. (particularly for isotactic polypropylene) where clarifying agents (nucleating agents) are added for purposes of promoting a finer scale superstructure which leads to a higher clarity product resulting in a higher margin of profit. A higher nucleation density also tends to enhance not only clarity but in addition, generally improves mechanical properties—another desired side benefit from higher nucleation.

Although the bulk scattering effects discussed above are important, it is now generally recognized and accepted that the primary cause of poor optical properties (i.e., high haze) in blown films is the surface roughness of the film.^{2-4,12,13} If indeed surface asperities exist on the scale of the

wavelength of light, considerable diffuse reflection and refraction effects occur providing enhanced turbidity. Film or product smoothness is critical to decrease turbidity as promoted by surface effects. For molded articles, surface roughness can often be minimized by appropriate mold design and suitable release agents. However, in the case of free-surface flows such as film blowing, the surface roughness principally has two main causes, viz., melt flow-induced phenomena and crystallization, the latter of which can be of great importance to surface texture.

Surface roughness due to melt flow-induced phenomena occurs as a consequence of the polymer melt elasticity and can range from the fine-scale surface irregularities (often referred to as extrusion haze) to more gross scale surface irregularities such as sharkskin melt fracture, “orange-peel” and “applesauce” textures.¹ The severity of these various surface irregularities generally increase with output (shear) rate and are readily observed in the melt bubble immediately above the die itself. Hence, there is often a balance in terms of what process speeds can be utilized to minimize surface irregularities resulting from these rheological instabilities. The crystallization-induced surface roughness phenomena in blown films, although known to occur, are much less understood.

For the sake of completeness, it should be added that inhomogeneities such as gels, inorganic particulate additives (such as talc or silica), scratches, etc. can also contribute to poor clarity as a result of added light scattering either in the bulk or reflection/refraction effects at the surface or some combination thereof.

Recently, we have undertaken a thorough study of the optical haze (or its inverse, clarity) for blown polyethylene films. Specific focus has been directed toward a more complete understanding of controlling the contribution from the surface roughness to film haze and it is this topic that we address. Of particular interest is the recognition that the newer metallocene narrow molecular-weight distribution polymers tend to provide lower relaxation times within the melt process thereby leading to the development of a somewhat spherulitic-like superstructure in the final blown film—a point evidently not well recognized by the “blown film” community. This superstructure can play a major role in causing haze and it will be considered as a focal point for the contents of this report.

EXPERIMENTAL

Melt Rheological Characterization

The resin samples were compression molded at 182°C for a total of 3 min. The samples were allowed to melt at a relatively low pressure for 1 min and then subjected to a high molding pressure for an additional 2 min. The molded samples were then quenched in a cold (room temperature) press. For rheological characterization, 2 × 25.4 mm diameter disks were stamped out of the molded slabs.

Small-strain (10%) oscillatory shear measurements were performed on a Rheometrics Scientific, Inc. ARES rheometer using parallel-plate geometry to obtain the complex viscosity (η^*) versus frequency (ω) raw data. The test chamber of the rheometer was blanketed in nitrogen to minimize polymer degradation. The rheometer was preheated to the initial temperature of the study. Upon sample loading and after oven thermal equilibration, the specimens were squeezed between the plates to a 1.6-mm thickness and the excess was trimmed. A total of 8.0 min elapsed between the time the sample was inserted between the plates and the time the frequency sweep (0.03–95 rad/s) was started. The $|\eta^*|$ versus ω data were then curve fitted using the modified three parameter Carreau-Yasuda empirical model to obtain the zero shear viscosity, η_0 . Details of the significance and interpretation of the Carreau-Yasuda model may be found elsewhere.^{14–17}

Melt Index (MI) was measured in accordance with ASTM D-1238, condition F (190°C, 2.16 kg). Density was measured using density gradient columns in accordance with ASTM D-1505.

Molecular Weight Measurements by Gel Permeation Chromatography

Molecular weight distribution (MWD), molecular weight averages (M_n , M_w , M_z), and polydispersity (M_w/M_n) were obtained using a Waters 150 CV Plus Gel Permeation Chromatograph using trichlorobenzene as the solvent with a flow rate of 1 mL/min at a temperature of 140°C. BHT at a concentration of 0.5 g/L was used as a stabilizer in the solvent. An injection volume of 220 μ L was used with a nominal polymer concentration of 5 mg/3.5 mL of solvent (at room temperature). The column set consisted of two Waters Styragel

HMW 6E mixed-bed columns. A broad-standard integral method of universal calibration was used based on a Phillips Marlex BHB 5003 broad linear polyethylene standard. Parameter values used in the Mark-Houwink equation ($[\eta] = K \cdot M^a$) for polyethylene were $K = 39.5(10^{-3})$ mL/g and $a = 0.726$.

Blown Film Processing

All the blown film samples were made on a laboratory-scale blown film line using typical linear low-density (LLDPE) conditions as follows: 100-mm (4-in.) die diameter, 1.5-mm (0.060-in.) die gap, 37.5-mm (1.5-in.) diameter single-screw extruder fitted with a barrier screw with a Maddock mixing section at the end ($L/D = 24$, 2.2:1 compression ratio), 115 RPM screw speed [approximately 27 kg/h (60 lb/h) output rate], 2.5:1 blow up ratio, “in-pocket” bubble with a “freeze line height” between 20–28 cm (8–11 in.), 190°C (375°F) barrel and die set temperatures, and 1-mil (25-micron) thick film. Cooling was accomplished with a Dual Lip air ring using ambient (laboratory) air at approximately 25°C (75–80°F). These particular processing conditions were chosen because the film properties so obtained are representative of those obtained from larger, commercial scale film blowing conditions.¹⁸

Cast Film Processing

The cast films for the study involving metallocene resin H spiked with the high M_w Sample P, were obtained as follows. The cast films were all made on a Randcastle Microtruder CF (model RC-0625) which consisted of a tabletop 16-mm (5/8-in.) single screw extruder. The extruder was fitted with a 127-mm (5-in.) wide slot die with a die gap of 0.5 mm (0.020 in.). The extruder and die temperatures were maintained at 204°C (400°F) and 215°C (420°F), respectively, resulting in a melt temperature of 196°C (385°F). The screw speed was adjusted to maintain a constant output rate of approximately 520 g/h. The melt as it exited the die was quenched using a pair of high velocity air knives, held 25 mm (1 in.) above and below the melt and at a distance of 100 mm (4 in.) downstream from the die exit. The film, subsequent to crystallization and solidification, was taken up through a pair of primary and secondary rollers onto a film winder. The take-up speed was adjusted to maintain a nominal film thickness of 75 microns (3 mils) for all samples.

Structural and Optical Techniques Utilized

Atomic Force Microscopy (AFM)

AFM micrographs were obtained with the use of a Digital Instruments Nanoscope III Scanning Probe Microscope operated in tapping mode. Nanosensor TESP single-beam cantilever tips possessing force constants of 35 ± 7 N/m and oscillated at frequencies of ca. 290 kHz were used. The films were placed on glass slides using double-sided tape with raster scanning of the sample done parallel to the machine direction of the film.

Small-Angle Light Scattering (SALS)

SALS was accomplished using a HeNe laser with a wave length of 632.8 nm. Only the H_v mode was used which represents where the polarization direction of the incident beam is vertical, as is the machine direction (MD) of the films, while the analyzer is horizontally oriented, respectively. The sample-to-film distance was 10 cm unless otherwise stated within the text or figure captions. Further details of this technique are described in detail elsewhere.¹⁹

Differential Scanning Calorimetry (DSC)

DSC measurement was performed with a Perkin-Elmer DSC7 operating at cooling rates of 5°C/min, 30°C/min, or 80°C/min using sample weights ca. 5 mg. Sample temperatures were raised to 160°C for 10 min followed by cooling to follow crystallization. The samples were then reheated to 160°C for 15 min followed by a second crystallization run. In limited cooling studies on samples A, B, and C, trends within the DSC cooling data remained the same for the three cooling rates used as well as being independent of time spent in the melt. Heating scans were also done using a heating rate of 30°C/min with samples sizes of either 7.5 or 5 mg. Instrument calibration was done using indium and tin samples. Baseline corrections were applied the standard Perkin-Elmer software package.

Transmission Electron Microscopy (TEM)

Transmission electron micrographs were taken with a Philips EM420 scanning transmission electron microscope (STEM) operated in the transmission mode at 100 kV. Samples were prepared by staining with chlorosulfonic acid^{20,21} to greatly increase the electron density of the amor-

phous phase, thus providing sufficient contrast between the amorphous and crystalline phases. The samples were placed in the chlorosulfonic acid solution for approximately 2 h at 60°C followed by washing and drying before being microtomed at room temperature. As a result the micrographs display darkened amorphous regions and lighter crystalline lamella.

Haze Measurement

Haze is that percentage of the total transmitted light which, in passing through the specimen, is scattered from the incident beam by more than 2.5°. The haze (%) was measured in accordance with the procedures specified in ASTM D 1003-97. It should be noted here that haze is a different measure than clarity (also referred to as transparency) because the latter, in contrast, is the percentage of incident light which, in passing through the specimen, is deflected by less than 0.1° from the axis of the incident light. The measurements were made on a Haze Gard *Plus*TM instrument (model 4725) made by the BYK-Gardner® Company.

To separate the measured total haze into its bulk (or internal haze) and surface (or external haze) components, the following procedure was used. First, the haze of the as-blown film sample was measured. This is the total haze of the film. Then a very thin layer of a silicone oil [A-Series oil, refractive index (n) = 1.512 from Cargille Oil Co.] of similar refractive index to that of the film was applied to both sides, i.e., the outside surface of the bubble and the inside surface of the bubble. The haze was measured again. This value is the bulk contribution. Finally, the difference between the total haze value and bulk haze value provided the surface haze contribution directly.

Materials

Several different metallocene (resins A, B, C, E, F, G, and H) and Ziegler-Natta (Z-1 and Z-2) catalyzed LLDPE resins were used in this study. In addition, a chromium catalyst resin (resin P) was used in the second part of this study as a minority blend component. The basic resin specifications, molecular, and thermal characteristics are provided in Table I.

RESULTS AND DISCUSSION

Details regarding molecular weight, rheological parameters, melting, and melt crystallization

Table I Molecular Weight Characteristics and Thermal Transition of the Resins Used in This Study

Resin	A	B	C	E	F	G	Z-1	Z-2	H	P
Melt index (g/10 min)	1.0	1.5	2.8	1.0	1.2	1.2	0.97	0.94	2.0	0.3
Density (g/cc)	0.918	0.920	0.930	0.917	0.918	0.934	0.919	0.934	0.926	0.923
M_n (kg/mol)	42.5	39.1	36.1	41.8	44.8	45.4	26.4	27.4	39.7	11.1
M_w (kg/mol)	100.9	86.13	80.5	108.3	103.1	108.3	129.9	119.6	85.7	182.9
M_z (kg/mol)	199.1	162.27	162.1	227.8	207.5	224.6	575.4	444.5	167.3	1406.9
M_w/M_n	2.37	2.20	2.23	2.59	2.30	2.39	4.92	4.36	2.16	16.5
T_m (°C)	111	113	119	114	116	128	125	127	120	122
T_c (°C)	88	88	95	93	93	101	101	103	95	100
Recoverable shear strain $\times 1E3$	22.6	5.9	4.8	12.9	10.6	5.1	101.8	108.1	3.7	438.9

temperatures for the individual resins are given in Table I. These will be utilized in subsequent discussion. Using the procedures given above for determining film haze, the separate contributions of surface versus bulk haze were determined. These results are given in Table II and clearly show that of the eight single-component blown film samples investigated, the surface haze contribution distinctly dominates the optical properties. It is noted that once the surface haze is eliminated through the refractive index oil matching, the bulk haze for many of these materials is low enough to indicate that the films investigated are near to very optically clear materials! It is also seen that when the percent of surface haze is determined relative to the total haze, the surface contribution is at least 62% and often exceeds 80%. Hence, the issue is what type of surface irregularities exist on such blown films that cause the majority of haze—do they arise from rheological instabilities, the nature of the crystal texture that occurs at the film surface, or some other origin? To address this, Figure 1(a–c) provides AFM micrographs of a relatively low magnification scale for samples A–C, respec-

tively. These three samples were selected because they systematically vary in their surface contribution to haze with sample A being the least and sample C being the greatest. In this series, note the distinctly enhanced surface roughening effect as one proceeds from sample A to sample C. Figure 2(a–c) also provides the general profilometry scans of typical “profiles” of the surface of these same respective samples to help quantify the magnitude and frequency of the height perturbations. Certainly, both Figures 1 and 2 illustrate the variation in surface textures (and associated scale lengths) and its strong correlation with the optical data in Table II for these same three materials. It should be recognized, particularly for the micrographs presented in Figure 1(b,c), that the surface irregularities do not display the typical textures that are generally noted when melt rheological effects such as “sharkskin” melt fracture are induced. Rather, these figures suggest some form of nearly isotropic texture and therefore higher level magnifications were used. To illustrate the nature of the morphological entities responsible for the surface roughening effect, Figure 3(a) shows both the height and phase images

Table II Contributions to the Total Haze for the Polyethylene Blown Films Used in This Study

Film	A	B	C	E	F	G	Z-1	Z-2
Total haze, H (%)	2.47	19.43	59.27	13.40	14.87	25.63	11.37	15.03
Bulk haze, B (%)	0.93	1.86	9.64	1.22	1.54	3.14	1.72	3.21
Surface haze, S (%)	1.54	17.57	49.62	12.18	13.33	22.49	9.65	11.82
S/H $\times 100$ (%)	62.3	90.4	83.7	90.9	89.6	87.7	84.9	78.6
Spherulite diameter (μm)	1.7 ^a	4.3	5.6	3	2.4	NA	NA	NA

^a The spherulitic radius is a rough estimate because of the difficulty in determining the maximum intensity in the SALS pattern. In addition, NA for spherulite diameter implies that a maximum was not able to be found, however a highly distorted H_v pattern from a structure that scattered at extremely large angles (i.e., smaller structure).

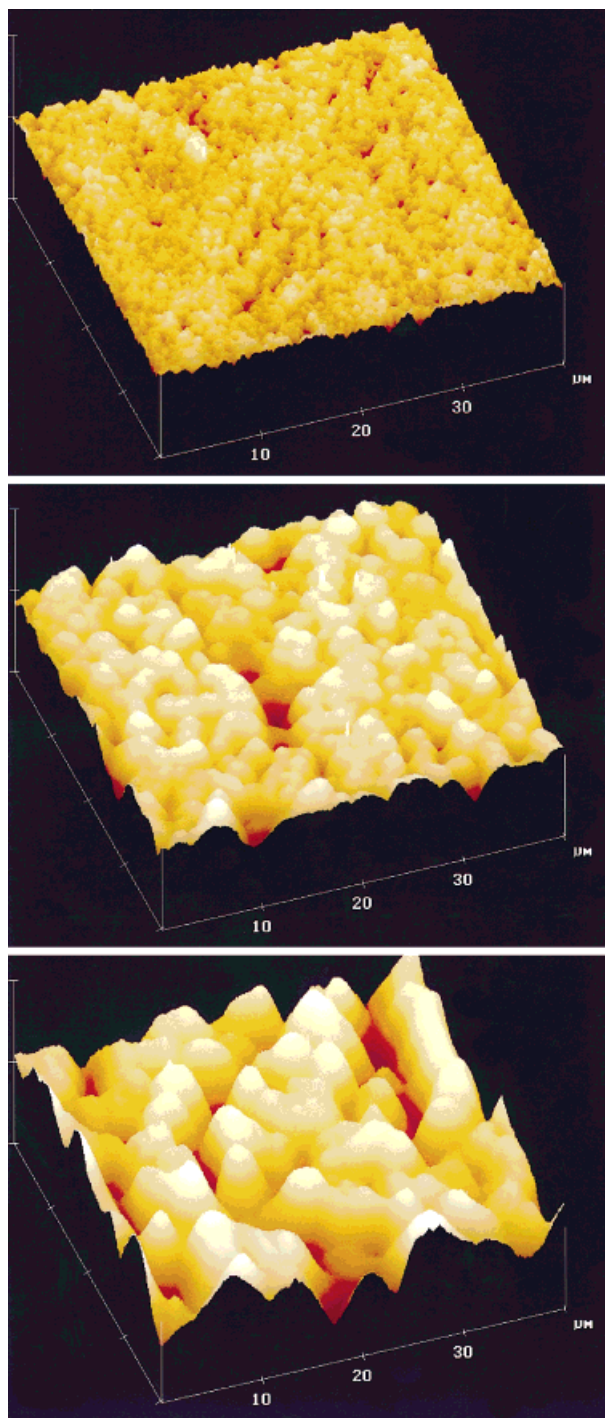


Figure 1 AFM tilted height images of blown films (a, top) sample A, (b, middle) sample B, and (c, bottom) sample C. Scales of the images are $800 \mu\text{m}$ (vertical) $\times 40 \mu\text{m} \times 40 \mu\text{m}$.

obtained from a region of sample C that displays the highest level of surface haze. Surprisingly, one notes that there are distinct spherulitic-like

superstructures that particularly stand out in the height image whereas the phase image displays a general lamellar texture expected from spherulitic-like entities. In contrast, the same magnification AFMs obtained in both the height and phase are shown for sample A in Figure 3(b), the sample with the lowest surface haze contribution. Here, whereas some signs of a much smaller superstructure are noted, this being about $1 \mu\text{m}$ in size, one also observes that the lamellar texture is less distinct but certainly present. Although not shown, sample B displays intermediate size superstructures similar to sample C. These micrographs clearly support the presence of a distinct somewhat spherulitic-like superstructure that occurs on the order of a few microns. Again this is not typical of surface irregularities promoted by melt fracture effects that are often used as the argument to account for surface haze. Such morphological features are in great contrast to the blown or tubular (blow-up ratio 1.0) film textures commonly reported whereby a more partially stacked lamellar or row structure occurs having some preferential orientation but where no significant larger scale superstructure is observed.^{22–26}

The AFM method, however, is a surface technique and although this is critical to address the

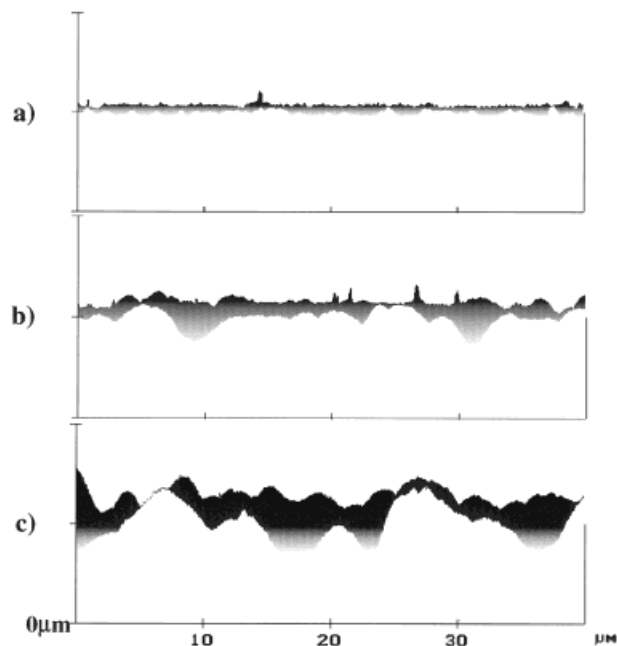


Figure 2 General profilometry scans of blown films (a) sample A, (b) sample B, and (c) sample C. The vertical axis range is $800 \mu\text{m}$ whereas the horizontal axis is $40 \mu\text{m}$.

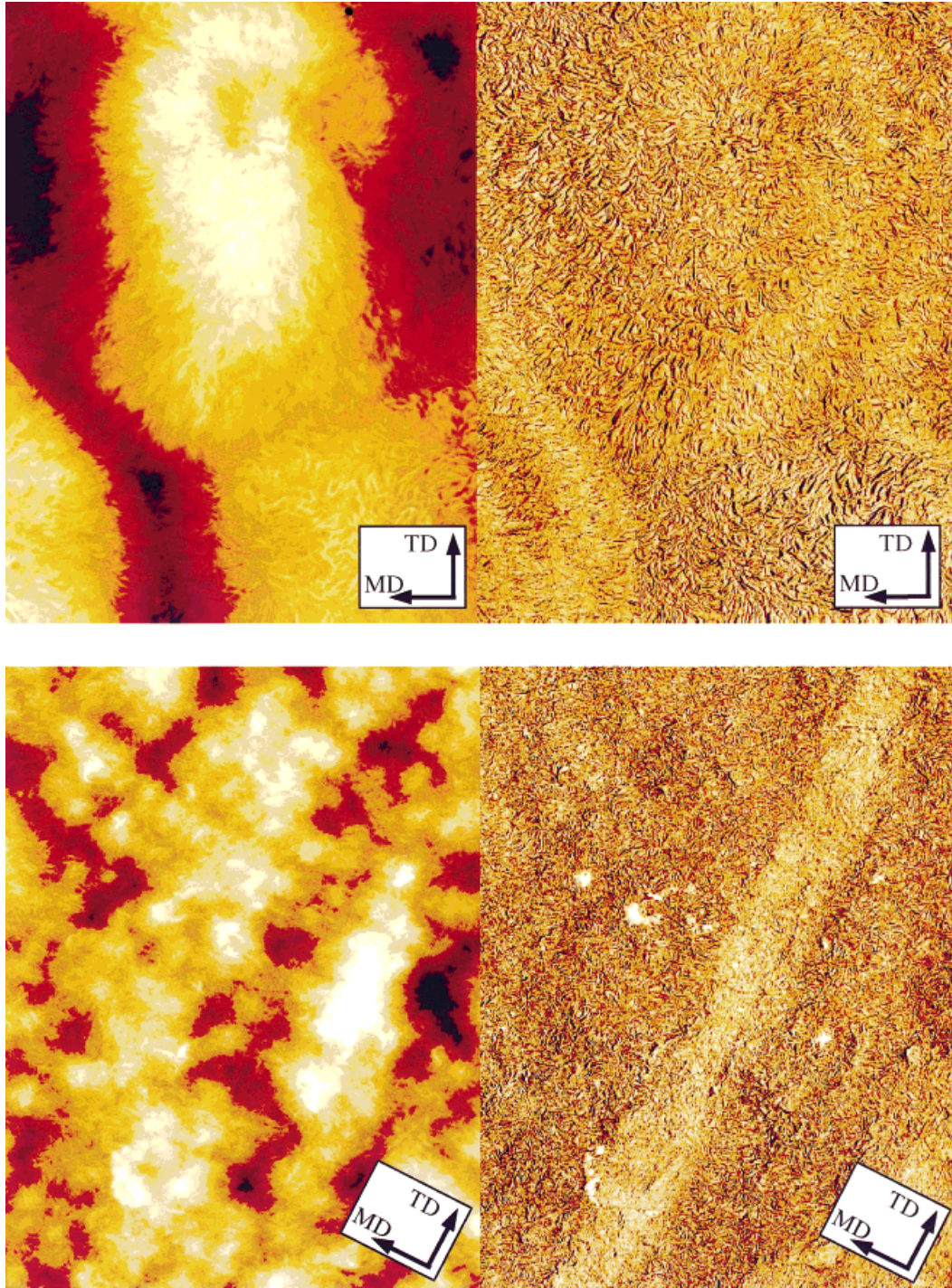


Figure 3 AFM height (left) and phase (right) images of blown films (a, top) sample C and (b, bottom) sample A. Images are $10\ \mu\text{m}$ (vertical) \times $7\ \mu\text{m}$ (horizontal).

features of surface roughness stated above, a major question is whether this suspected superstructural texture is truly a bulk phenomenon or not.

To provide further support for the general spherulitic-like arrangement of lamellar textures, i.e., it should be more random than a stacked or

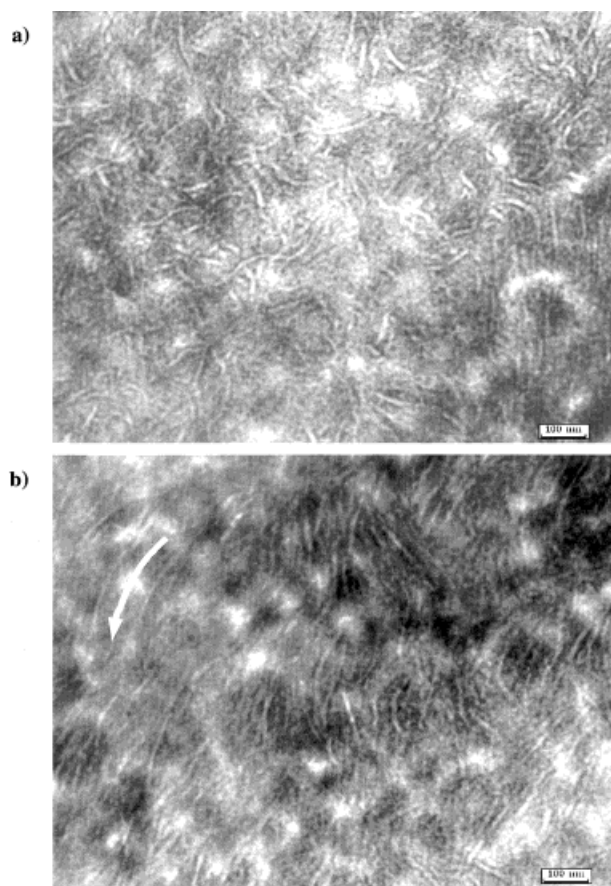


Figure 4 TEM micrographs of (a) sample B and (b) sample C. Note in sample C an arrow indicates the radial direction and twisting of a specific lamellae whereas in sample B a more random lamellae morphology occurs.

oriented lamella structure, two TEM micrographs are shown in Figure 4(a,b) for samples B and C, respectively. Here it is distinctly observed that for sample B, the lamella are generally randomly oriented whereas in sample C, there are even signs of the lamella extending and potentially twisting (see arrow) along a radius that would correlate to the radius of the spherulitic-like superstructure as seen in Figure 3(a). In addition, optical microscopy suggested support for this morphology but resolution limits hindered good imaging of all films. However, the very critical method to distinctly establish the confirmation of these superstructures as being optically anisotropic spherulitic-like bodies was through the use of SALS. This technique, developed in 1960 by Rhodes and Stein and addressed considerably in subsequent publications by these same cowork-

ers^{5,8,9,27–29} and others,^{2,7,10,16,30,31} is particularly effective in denoting the presence of optically anisotropic superstructures.

The specific blown films studied in this investigation are amenable to SALS studies because their bulk scattering is relatively low, thereby minimizing secondary scattering effects. Figure 5(a–f) shows the H_v SALS patterns for the blown film samples addressed in this study. As discussed elsewhere,¹⁹ the origin of the H_v scattering arises from optical anisotropy associated with the morphological texture. From these, one sees there is very distinct conformation of the spherulitic-like texture as noted from the sharp near “four leaf clover” patterns observed in the majority of

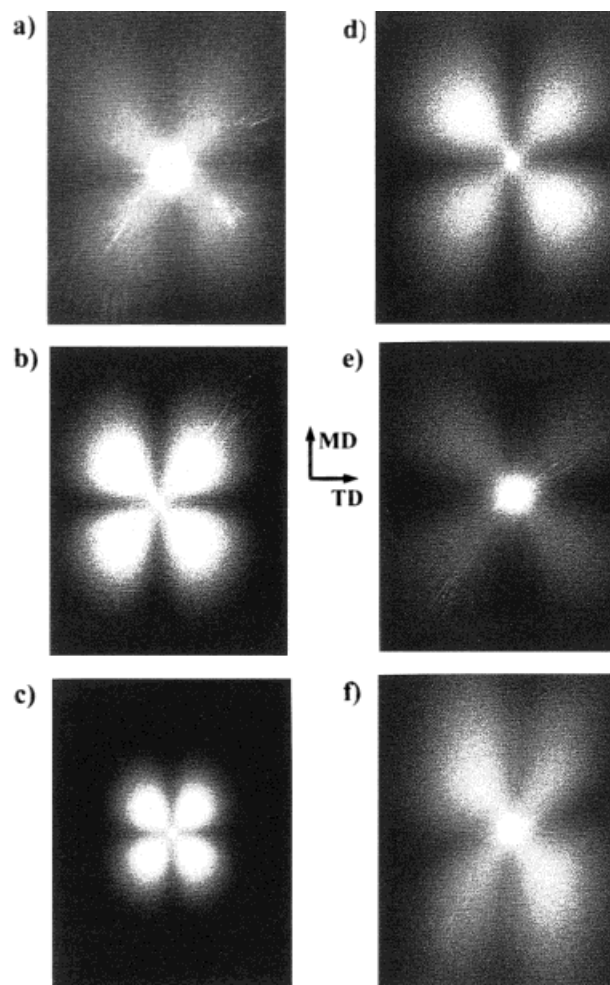


Figure 5 SALS H_v patterns of blown films (a) sample A, (b) sample B, (c) sample C, (d) sample E, (e) sample F, and (f) sample G. All sample-to-film distances are 10 cm with the exception of sample A which is 5 cm. The MD is along the long axis of the SALS patterns.

Table III Estimated Spherulitic Diameters Based on SALS Patterns for Some Samples Studied

Resin	A	B	C	E	F	G	Z-1	Z-2
Spherulite diameters (μm)								
For blown film	1.7 ^a	4.3	5.6	3.0	2.4	NA	NA	NA
For quench sample	5.7	9.4	10.2	—	—	—	—	—
For slow cool sample	6.7	9.6	10.6	—	—	—	—	—

^a The spherulitic radius is a rough estimate because of the difficulty in determining the maximum intensity in the SALS pattern. In addition, NA for spherulite diameter implies that a maximum was not able to be found, however a highly distorted H_v pattern from a structure that scattered at extremely large angles (i.e., smaller structure).

these films. It is also observed in most cases that the H_v patterns are slightly “deformed,” i.e., they show distinct twofold symmetry in contrast to near fourfold symmetry thereby implying a small level of deformation of the superstructural elements [see Fig. 5(c)]. To be sure the reader notes this twofold versus fourfold symmetry of many of the H_v patterns, the reader need only rotate the manuscript photo 90° in the plane to observe this feature [e.g., Fig. 5(c)]. This twofold symmetric pattern, as coupled to the well known theory of H_v SALS behavior, surprisingly indicates that the long axis of the superstructural element lies more along the “hoop” or transverse direction (TD) of the blown film process in contrast to the MD. It should be pointed out here that this perpendicular orientation of the superstructure is not a result of the hoop orientation promoted during the film blowing operation. The basis for this statement rests on the fact that the majority of the blow up in the bubble, which would be largely responsible for the TD orientation, occurs before the onset of crystallization (i.e., the freeze line height). Furthermore, when the films are freely annealed at higher temperature, the percent shrinkage in the TD or hoop direction is negligible. No change is observed in the H_v patterns as a result of such annealing processes even if taken very near the melting point. A later portion of this report will address the possible origin of this twofold symmetric superstructure.

As is well established, the average radius, R , of an anisotropic spherulite can be determined from the H_v pattern^{19,32} by use of the relationship:

$$4.13 = \frac{4\pi R}{\lambda_m} \text{Sin}(\theta_{\text{max}}/2) \quad (1)$$

where λ_m is the wavelength in the medium and θ_{max} is the radial scattering angle defined by the

maximum in the scattering intensity in any lobe of the fourfold symmetric H_v pattern. The value of λ_m is determined by dividing the wavelength of the incident beam (632.8 nm) by the average refractive index of the polymer (1.51).

As noted in Figure 5, several of the measured H_v patterns do not show a major deviation from fourfold symmetry although some slight orientation occurs in the transverse or hoop direction of the film. Hence, Eq. (1) was still used to *estimate* the diameter of the anisotropic superstructures for many of the films. These results are given in Table III and the general diameters obtained quite closely match the values determined by AFM. Note that these comparisons obtained by either AFM and H_v scattering only best apply to those systems that display the less oriented H_v patterns shown in Figure 5.

Reinspecting Figure 5 for the remainder of the SALS patterns not yet addressed, one notes that for sample A (lowest surface haze material) the presence of an anisotropic superstructure is also apparent from the SALS pattern. However, no distinct maximum in any of the four lobes occurs thereby making it impossible to clearly establish a superstructure size. However, the scattering does occur at distinctly higher angles relative to samples B and C (note that a much smaller sample to film distance was used to record the H_v pattern for sample A), thereby implying that sample A possesses smaller superstructural elements as was verified earlier by AFM [recall Fig. 3(d–e)]. Sample E, which also possesses considerable surface haze, displays a near symmetric fourfold pattern and provides a superstructure on the order of $3 \mu\text{m}$ as estimated by SALS. The H_v pattern for sample F is less distinct than sample E yet does display a near fourfold symmetry. Interestingly, sample G shows an even more perpendicularly oriented superstructure to the MD direction

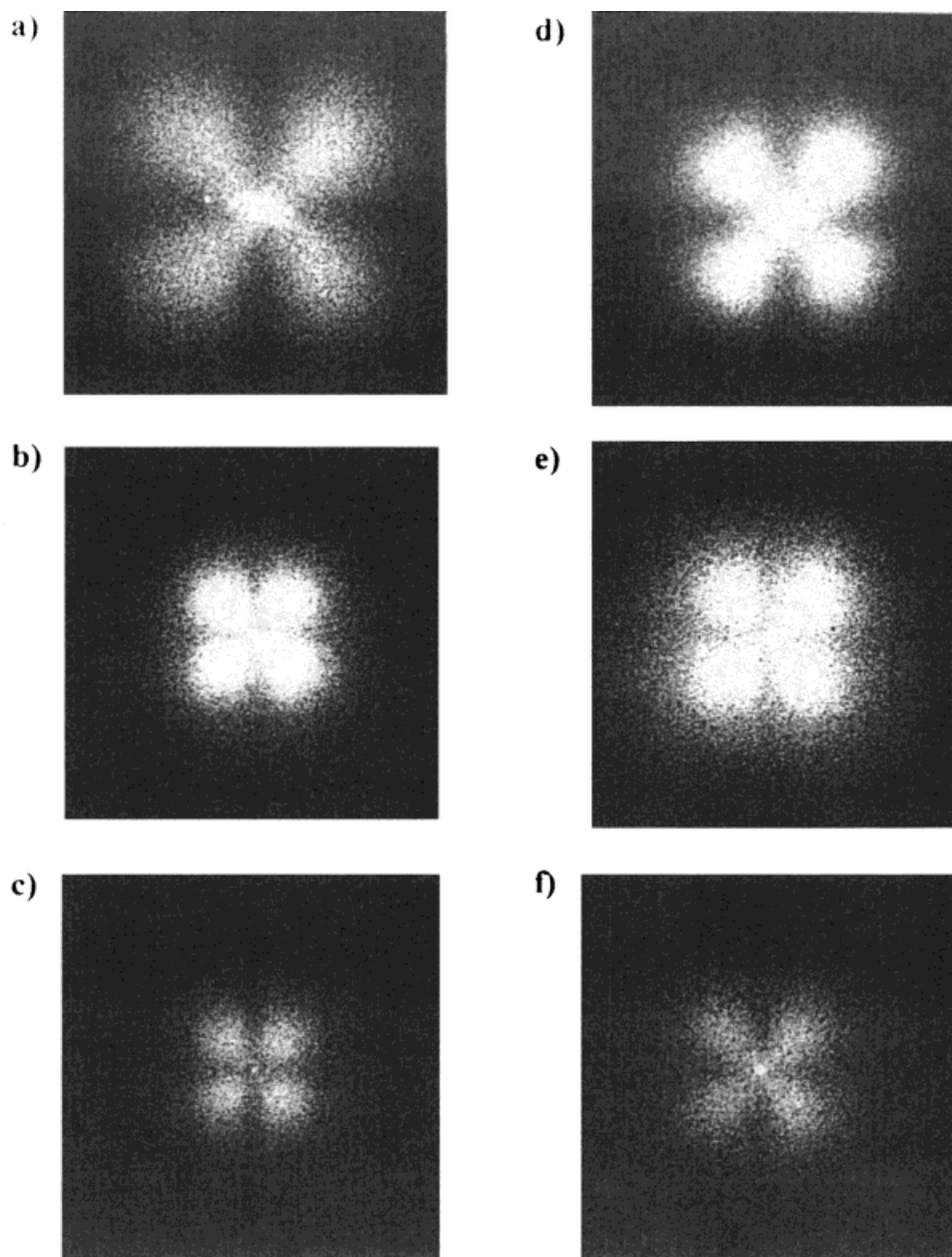


Figure 6 SALS H_v patterns of undeformed compression molded quenched samples from sample resins (a) A, (b) B, (c) C and slow cooled samples (d) A, (e) B, and (f) C. The patterns were taken with sample-to-film distances of 16 cm.

and did not allow easy estimation of superstructural size by use of the SALS approach. However, SALS theory developed by Stein and coworkers,³³ Samuels,^{7,32} and Hashimoto and coworkers^{10,34} have attempted to quantitatively account for how such superstructure is deformed from tracking the changes in the SALS patterns as a function of draw ratio in uniaxially deformed systems. Fi-

nally, for the two films produced by using the broader molecular weight distribution Ziegler-Natta resins, Z-1 and Z-2, although there were signs of some very weak azimuthal dependence to the H_v scattering, no discrete pattern was noted to confirm the presence of a distinct superstructure and these patterns are therefore not included in Figure 5.

It might be pointed out in passing that all the associated resins A–Z-2 (excluding H and P) were also compression molded into thin films and crystallized quiescently whereby all displayed the typical H_v light scattering patterns expected of unoriented optically anisotropic spherulites. To illustrate this point, Figure 6(a–f) shows the H_v patterns obtained from the respective quenched and slow cooled samples of only materials A, B, and C produced by this compression molding process. As expected, lower-angle scattering is observed for each respective sample when prepared by the slow cool process which leads to lower nucleation density and somewhat larger superstructure. While for the “slowly cooled” thermal history, sample C tended to display the largest superstructure (smaller H_v pattern), its size is also nearly equal to those of samples A and B when prepared by the slow cooling process although sample A certainly displays a somewhat smaller superstructure when prepared by quenching [compare Fig. 6(a) with Fig. 6(d)].

In summary of the data presented thus far, we reiterate that the surface haze is the dominating contributor to the total haze behavior of these systems in blown film form and is attributed to the development of superstructural spherulitic-like elements. The exceptions are samples Z-1 and Z-2; these will be addressed later. However, note that the MI values for all eight materials in Table I are quite similar except for sample C, which is higher. It is worth reemphasizing here that all samples in Table I, excluding Z-1 and Z-2 (and the broad MWD chromium catalyzed resin P), represent narrow MWD metallocene polymers. This latter statement is strongly supported by the dynamic rheological data presented in Figure 7. This shows that the $\log(|\eta^*|) - \log(\omega)$ data distinctly display that samples Z-1, Z-2, and P indicate higher viscosity at low frequency and experience the onset of shear thinning at much lower frequencies than do the narrow distribution metallocene resins. This major difference in behavior is influenced by the molecular weight distribution breadth and the corresponding shorter relaxation time behavior associated with the metallocene materials. Furthermore, it should also be noted that the resins in Table I (with the exception of resin P) contain no long chain branching. A log–log plot (not shown here) of the zero shear viscosities versus the weight-average molecular weights, M_w , for the resins in Table I (again excluding resin P) revealed that the data all fall on

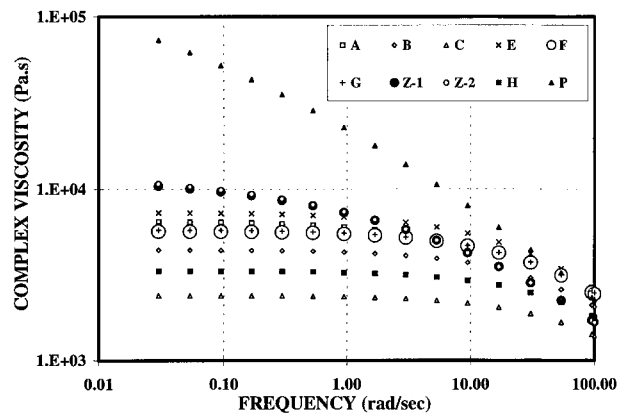


Figure 7 Plot of $\log |\eta^*|$ versus $\log(\omega)$ for the resins studied (same resins listed in Table I).

a straight line with a slope of about 3.4. This 3.4-power dependence of the zero shear viscosity on M_w follows the well known empirical relationship for flexible linear polymers for M_w values greater than the critical entanglement molecular weight.^{16,35,36}

It is generally accepted that blown or tubular film processing of polyethylene resins possessing lower molecular weights and narrower molecular weight distributions often leads to preferential “ a ”-axis orientation.^{22–24,26,37} Wide angle X-ray scattering (WAXS) patterns obtained on samples A and C indicate that some slight “ a ”-axis orientation also exists, although it is hardly detectable. To illustrate this, Figure 8(a and b) is provided which shows the WAXS patterns for samples A and C, respectively. Note that sample A has the higher “ a ”-axis orientation but both materials display low orientation. Results for sample B (not shown) were intermediate between those of samples A and C. Low “ a ”-axis orientation was also observed of samples E–G as well, although the WAXS results are not shown here for brevity. In contrast, however, the two Ziegler-Natta broader MWD resins (samples Z-1 and Z-2) display a much more pronounced “ a ”-axis orientation as seen in Figure 8(c,d). AFM micrographs of the corresponding films of Z-1 and Z-2 also display no signs of superstructure although a distinct lamella texture is noted with some sign of these lamella being more preferentially perpendicular to the MD direction than purely random—see Figure 9 where the surface texture is shown for sample Z-2.

When polyethylene resins of higher molecular weight and broader molecular weight distribution

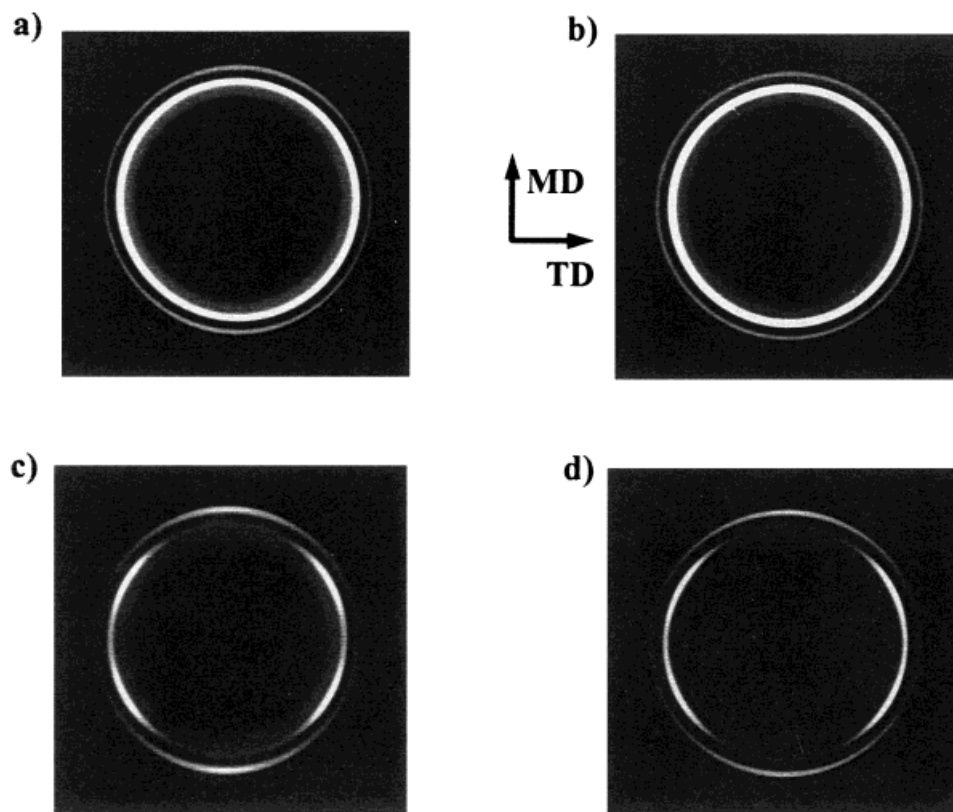


Figure 8 WAXS photographs of blown films (a) sample A, (b) sample C, (c) sample Z-1, and (d) sample Z-2. MD direction shown.

are processed into blown or tubular films, a fibril nucleated row or shishkabob-like texture has been reported by many researchers.^{38–40} Hence, the principal issue is: what has promoted the

major occurrence of a more spherulitic-like superstructural element in the present lower density metallocene materials that are not present in the two Ziegler-Natta resins of nearly comparable MI

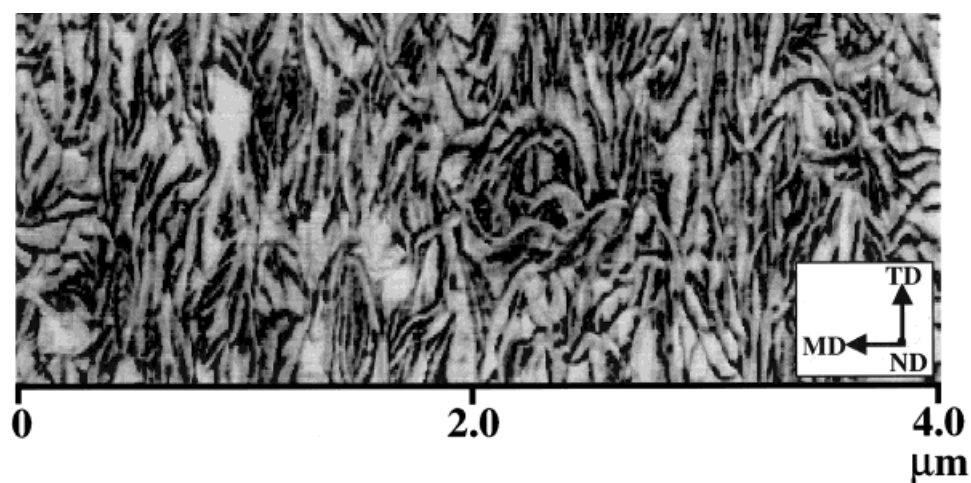


Figure 9 AFM phase image of the blown film Z-2 which uses a Ziegler-Natta catalyzed resin. MD direction shown.

Table IV Contributions to Total Haze and Spherulite Diameter for H Cast Roll Films with P Blend

Film	0 wt % P	3 wt % P	5 wt % P	8 wt % P	12 wt % P	15 wt % P	20 wt % P	30 wt % P
Total haze, H (%)	31.40	22.20	20.80	18.00	18.10	17.60	15.20	11.40
Bulk haze, B (%)	16.40	9.28	8.62	6.41	6.05	5.96	5.18	5.27
Surface haze, S (%)	15.00	12.92	12.18	11.59	12.05	11.64	10.02	6.13
S/H × 100 (%)	47.8	58.2	58.6	64.4	66.6	66.1	65.9	53.8
Spherulite diameter (mm)	6.8	3.2	2.8	2.1	1.4 ^a	NA	NA	NA
Recoverable shear strain × 1E3	3.7	25.5	41.2	NM	NM	NM	117.1	214.4

NM, not measured.

^a The spherulitic radius is a rough estimate because of the difficulty in determining the maximum intensity in the SALS pattern. In addition, NA for spherulite diameter implies that a maximum was not able to be found, however a highly distorted H_v pattern from a structure that scattered at extremely large angles (i.e., smaller structure).

when processed under essentially equal conditions? We propose that the induced superstructure in these materials results from a more rapid relaxation process (lower Deborah number) of the melt as the metallocene material proceeds from the die in the blown film process. It is recognized that metallocene materials, in general, have narrow molecular distributions and therefore lack the presence of high molecular weight fractions common to the typical Ziegler-Natta resins or chromium oxide-based materials (recall Table I). This major difference in molecular weight distribution can strongly influence elasticity and recovery or relaxation time accordingly. To indicate this difference in the resins investigated, an estimation of the recoverable shear strain was undertaken. Formally, the recoverable shear strain, γ_∞ , can be stated to be equal to:

$$\gamma_\infty = \frac{N_1}{2\tau} \quad (2)$$

where N_1 is the first normal stress difference and τ is the shear stress.⁴¹ At low frequencies, the recoverable shear can be estimated by:

$$\gamma_\infty \sim \frac{G'}{\omega|\eta^*|} \quad (3)$$

where G' represents the elastic part of the dynamic shear modulus whereas η^* and ω represent

the corresponding complex viscosity (using the well known Cox-Merz rule) and frequency, respectively.⁴¹ Applying this approximation in the low frequency range ($\omega = 0.03 \text{ s}^{-1}$), the values for recoverable shear strain of the respective eight resins are shown in Table IV. We observe that the values for the metallocene resins are distinctly lower than the two Ziegler-Natta resins, the latter of which provide blown films that show no signs of superstructural elements. These data provide very strong support for a much lower elastic character to the metallocenes as would be expected based on their lack of a high molecular weight tail component in contrast to the two Ziegler-Natta materials. This suggests why the two Ziegler-Natta resins do not promote a superstructural texture during processing. This is because of their longer relaxation time response (and thus a more elastic behavior than the metallocene materials) which limits their melt randomization and promotes a more oriented semicrystalline texture. In contrast, the metallocene resins, although of nearly equal MI, possess the ability to undergo relaxation more quickly (recall Fig. 7) and thereby develop a more “quiescent-like” texture following nucleation and growth of the crystalline phase. The fact that such a near “quiescent-like” morphology can develop in some polyethylenes during the film-blowing process, where the melt is undergoing a nonuniform biaxial stress under extremely rapid crystallization

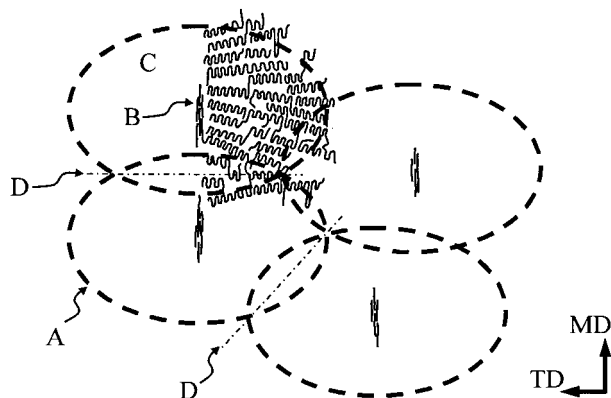


Figure 10 Model illustrating the nucleation of spherulitic-like morphologies on extended chain crystal nuclei. (The presence of some extended chain crystals has been assumed in this model without experimental proof.) (A) Outline of spherulitic-like region displaying anisotropy; (B) central fibrous or extended chain crystal; (C) folded chain lamellae nucleated on the extended chain crystal; (D) regions of spherulitic impingement. The lack of “*a*”-axis orientation (i.e., lamellar twisting) is *not* depicted in this illustration but does occur within the LLDPE films.

kinetics, has neither been recognized nor so well established before to the best of our knowledge.

As demonstrated by the earlier WAXS results, for even the case of the metallocene materials, there is some inherent “*a*”-axis orientation promoted in many of the blown films. Also as has been discussed, the SALS data clearly show that the long axis of the superstructural element is preferentially perpendicular to the MD axis. We view this as an indication that even in these metallocene materials, there is still some promotion of a partially fibril nucleated structure. The structure is not excessive and thereby only promotes a sheaf-like and near spherulitic-like superstructural development that has some preferential perpendicular orientation of its long axis to the MD direction.

A general and over simplified schematic of this model is indicated in Figure 10 and relates somewhat in nature to a model proposed much earlier by one of the authors in accounting for similar light scattering response promoted in strain induced crystallized superstructures promoted in cold drawn polyethylene terephthalate. It is to be made clear, however, that the conditions under which the inducement occurred for the superstructure proposed in the earlier reference is quite different than that originating in the blown

films discussed in this report. It should also be pointed out that Hashimoto and coworkers have prepared a related model (fan model) to account for perpendicular oriented H_v patterns as obtained from tubular (blow-up ratio 1.0) extruded poly(1-butene) film materials. Whereas certainly their model has relevance to our own study, our morphological textures (noted by AFM) display a more completely developed spherulitic-like superstructure, particularly the metallocene blown films and thus the reason for our proposed model.

To further lend support to the proposed explanation of the observed morphology on the blown 1 mil films, a related study with resin A was conducted using the melt cast process discussed in the processing section. While a constant shear rate was maintained, the film thickness, however, was controlled to be 1, 3, or 5 mils by adjusting the take-off speed. These respective cast materials were then studied with respect to their haze characteristics, crystal orientation as determined by WAXS, and their morphology as studied by both SALS and AFM. The results obtained by SALS are displayed first in Figure 11(a–c), and show no distinct sign of superstructure within the thinnest film. In the two thicker films, the spherulitic-like superstructure obtained is also oriented somewhat perpendicular to the draw direction; the reader should recall there is no blow-up ratio in this cast process, yet the perpendicular orientation is still noted! These results directly support the arguments provided to this point for the cause of the same perpendicular oriented type of superstructure being induced within the blown films. Although not shown here, the AFM of the thinnest sample distinctly showed signs of lamella being quite stacked and oriented perpendicular to the MD direction strongly supporting the reason no signs of a distinct superstructure entity above the lamellar level would have been observed by the SALS technique. Oriented stacked lamella, however, were not observed in the thicker materials. The corresponding WAXS patterns of the thinnest and thickest films are shown in Figure 12(a,b) and indicate a systematic decrease in uniaxial “*a*”-axis orientation as film thickness increases. The WAXS pattern for the intermediate thickness sample showed the “*a*”-axis orientation to be intermediate from that of the other two samples. This systematic decrease in “*a*”-axis orientation with thickness is undoubtedly attributed to a longer allowed time for relaxation to occur before crystallization because of

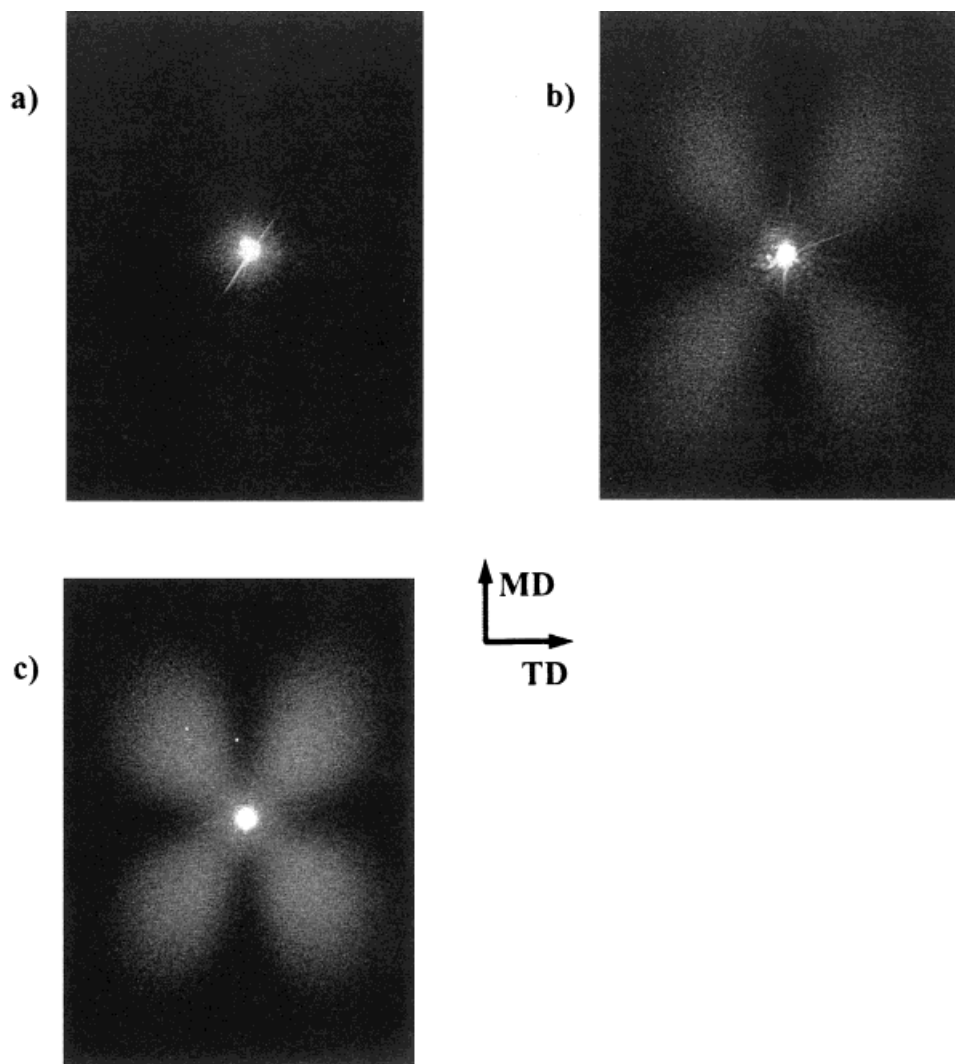


Figure 11 SALS H_v patterns of cast roll films with different film thickness values using sample A resin: (a) 1 mil film, (b) 3 mil film, (c) 5 mil film. The patterns were taken with a sample-to-film distance of 10 cm. The MD is along the long axis of the SALS patterns.

differences in heat transfer characteristics of the different thickness films and the line speed difference.

In summary, it is clear that the generally expected partially oriented or stacked lamella textures common to the Ziegler-Natta blown films are not found in many of the metallocene materials put through a similar melt process. Rather, because of their narrower molecular weight distribution and general lack of any long chain branching (at least in the metallocene resins studied herein), resulting in their lower elasticity and recoverable shear, these materials tend to

promote a more spherulitic-like superstructural element but which are postulated to be promoted by the lower but still partially oriented melt at the time of crystallization. The lack of a sufficiently high molecular weight tail to promote a higher recoverable shear or elasticity and longer relaxation time character is believed to be one of the major reasons that the metallocenes are able to display a somewhat more balanced morphology.

Our statements above strongly suggest that the importance of a high molecular weight tail is critical in helping to induce less development of a

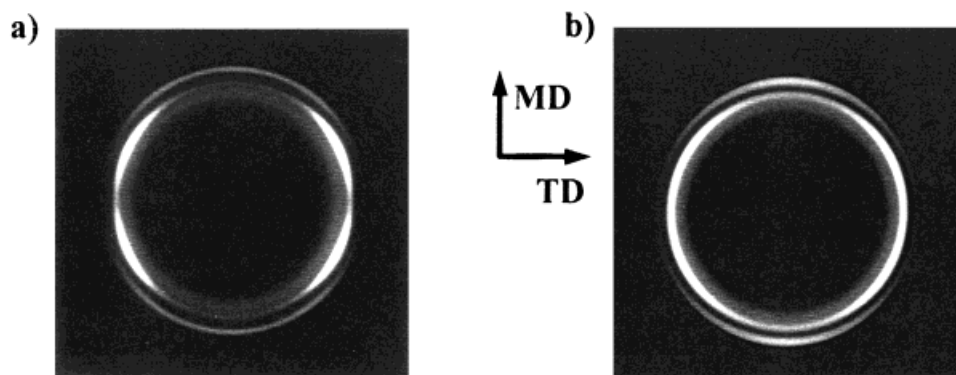


Figure 12 WAXS photographs of cast roll films with different film thickness values using sample A resin: (a) 1 mil, (b) 5 mil. MD direction is shown.

superstructure and therefore improve (lower) haze. This in turn suggests that a blend based on a narrow molecular weight distribution metallocene resin with a small amount of high molecular weight broad distribution material could also promote the elimination of superstructure if the high molecular weight tail blended component possessed a sufficient relaxation time to help induce a more stacked lamella texture. To test this hypothesis, the metallocene labeled as sample H in Table I was dry blended to different levels with a *particularly* broad molecular weight distribution resin made with a chromium catalyst—sample P of Table I.

It will be noted from Table I that sample H is quite similar to many of the metallocenes already addressed whereas sample P is quite different due both to its higher weight average molecular weight and distinctly broader molecular weight distribution (see Table I). For sample P, it is of value to note the magnitude of the z -average molecular weight, M_z , which is greatly influenced by the higher molecular weight fraction in the polymer. Because of this, one can distinctly anticipate a much broader spectrum of relaxation times and particularly much *longer* relaxation times in general than that possessed by sample H (or in fact any of the other metallocenes thus far addressed). Following the dry blending of sample H with different weight concentrations of sample P that varied from 3 to 30 weight percent, the materials were processed into cast films as described in detail in the Experimental section. A control film of pure sample H was also prepared and analyzed for comparative purposes. As anticipated, sample H in pure form displayed the expected H_v pattern indicating a spherulitic-like structure that was

also verified by AFM. It also displayed a reasonably large amount of surface haze as can be noted from Table IV where the results of this overall portion of the study are summarized. However, at just 3% weight concentration of the broad distribution chromium catalyzed resin P, the amount of haze was decreased as was the general surface roughness. Of particular note is that by the time the amount of the broad distribution blend component had reached about 10%, no clear sign of superstructure was easily observable by AFM and the surface roughness was decreased considerably relative to the pure H material! Whereas a *lamella* texture was still easily discernible from AFM observations, no micron size entities resembling spherulitic-like structures were noted; see Figure 13(a–d), which provide selected AFM height images. Furthermore, once the 20 weight percent level had been achieved, AFM clearly showed that there was a distinct stacking of lamella with the long axis of the lamella being aligned nearly perpendicular to the MD direction, similar to what would be expected for row-like structure; see Figure 14(a–b) which contrasts the AFM phase images of sample H containing 3 and 20 wt % of sample P. In fact, some signs of discrete “shish-like” fibril nuclei were noted on the surface of the 20 weight percent cast films! As expected, WAXS results distinctly showed an increasing amount of “ α ”-axis orientation as the amount of the broad distribution blend component increased; see Figure 15(a–d) which displays selected WAXS results. These data distinctly indicate a lengthening of the melt relaxation time behavior thereby accentuating the development of the “ α ”-axis orientation.

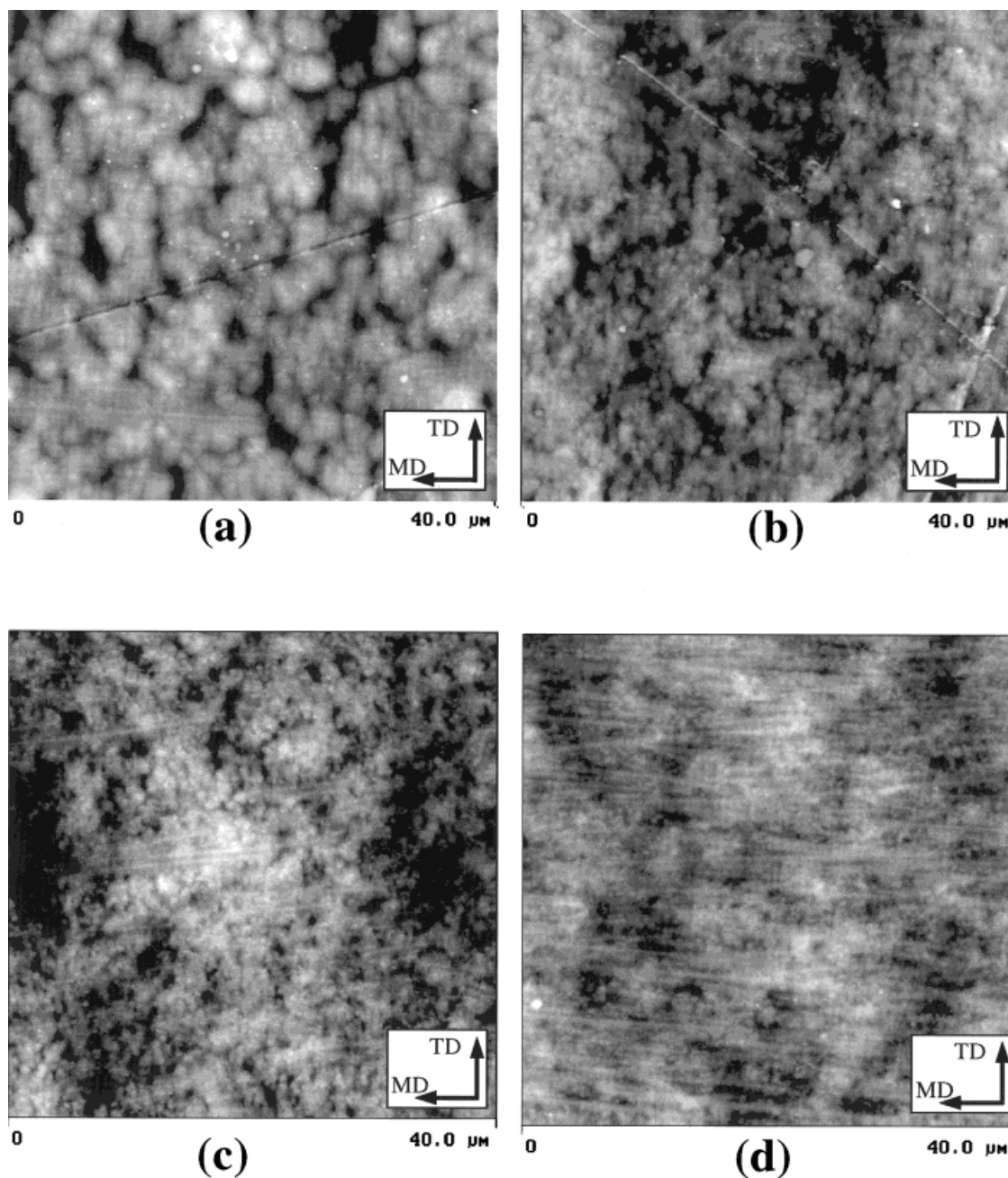


Figure 13 AFM height images of sample H cast roll films blended with varying wt % resin P concentrations: (a) 0 wt % P, (b) 5 wt % P, (c) 12 wt % P, (d) 30 wt % P. Images are $40 \times 40 \mu\text{m}$.

It is postulated that the higher molecular weight, broad molecular weight distribution component promotes more rapid nucleation and fibril-like nuclei that, in turn, promote additional secondary nucleation of the dominant metallocene H component leading to the observed structure. It is

also noteworthy that the inducement of the systematic changes in morphology with addition of sample P is clearly not attributed to a major change in supercooling effect for as noted in Table I, the T_m of sample P is not very different from that of sample H.

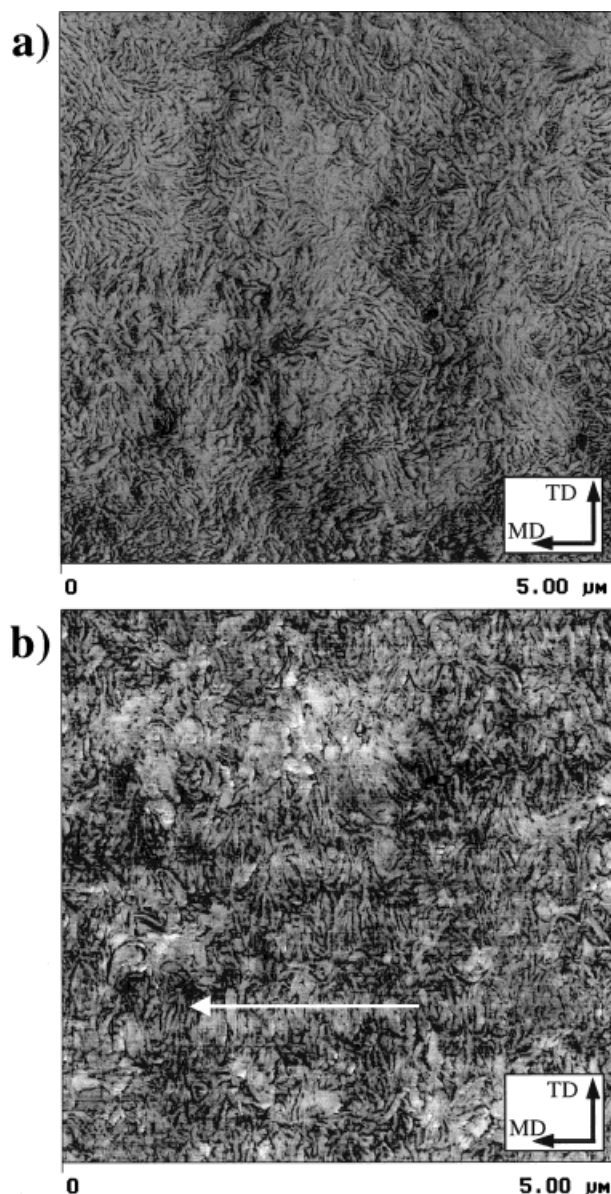


Figure 14 AFM phase images of sample H cast roll films blended with varying wt % resin P concentrations: (a) 3 wt % P, and (b) 20 wt % P. Note the random orientation of the lamellae in (a) whereas distinct stacked lamellae, as shown perpendicular to the arrow along the MD, are in (b).

Cooke and Tikuisis¹² reported identical results in an earlier study. They too had found that blending small levels of a high M_w , broad MWD resin to a LLDPE resin resulted in improved optical properties viz., lower haze and higher gloss of the base LLDPE resin. Although not related to the optical properties of thin

films, a very early study⁴² on the light scattering of mixtures of linear polyethylene resins also showed that the addition of even small amounts of a high M_w fraction to a lower M_w fraction resulted in a deterioration of the spherulitic morphology of the lower M_w fraction even in unoriented, isothermally crystallized samples.

Before concluding, it is important to state that at the very highest concentration level of sample P (30 wt %), it was noted that the surface roughness becomes more enhanced and this was easily discernible from the AFM micrographs. Specifically, the surface texture no longer provided a direct observation of lamella texture but rather a more roughened morphology was noted thereby providing hints of a localized melt fracture type response. This in fact seems logical and expected if there is a significant amount of fibril structure promoted through the nucleation and growth of the broad distribution component, particularly because the shear rate is highest at the wall. This can lead to “solid-like” behavior and promote signs of surface roughening of the remaining melt texture that has yet to solidify in the midst of the crystalline network-like structure nucleated by the broad distribution species. To give further support to our previous arguments concerning the alteration in surface texture through the increased relaxation times and associated recovered shear strain, we also provide the associated γ_∞ data on this same series of blends. This data is also presented in Table IV which shows how that parameter systematically increases with the weight percent increase in sample P—the broad distribution component content. We believe these results strongly support our conjecture that fine tuning the molecular weight distribution can have an extremely strong impact on the type of morphological texture induced which in turn influences surface roughness and associated optical haze.

CONCLUSIONS

From the above information we can *confidently state* that the one property that is dominated by the morphological entities discussed is haze, specifically surface haze due to the development of the superstructural entities that roughen the surface. It has led us to the conclusion that with increased nucleation, possibly promoted by resid-

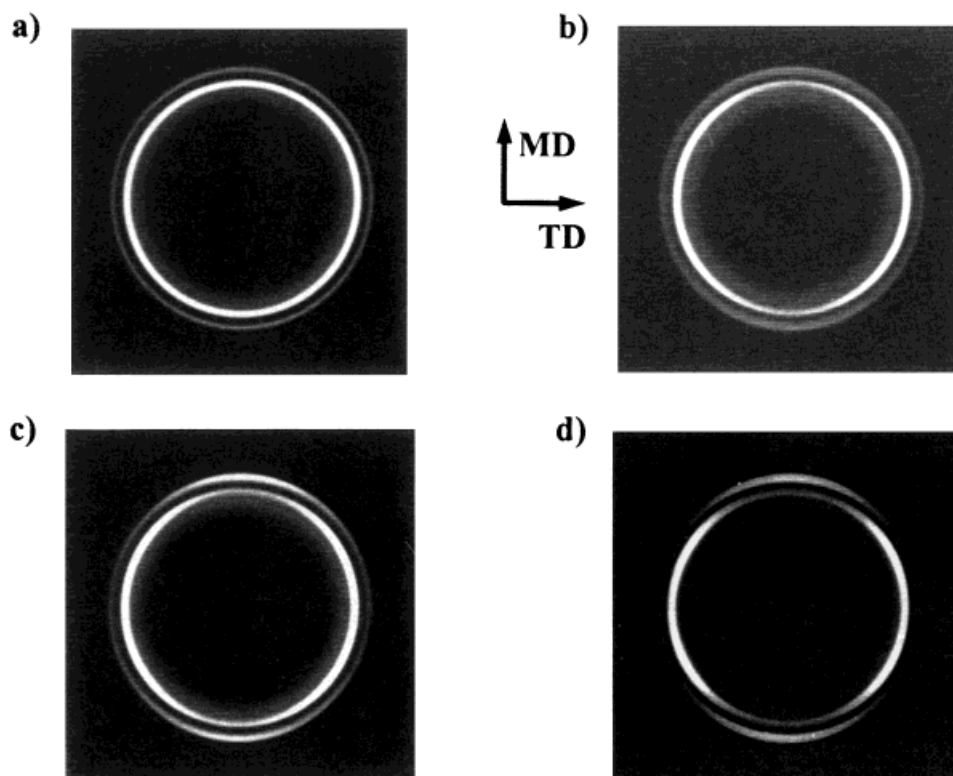


Figure 15 WAXS of cast roll films using sample H resin blended with varying amounts of the higher molecular weight P resin: (a) 0 wt % P, (b) 5 wt % P, (c) 12 wt % P, and (d) 30 wt % P. MD direction is shown.

ual orientation effects (but where such orientation is insufficient to induce the conventional row-like structure), the resulting superstructural elements are smaller which further results in a smoother film surface and thereby minimizes surface haze. This lower degree of surface roughness and surface haze yields a film with lower total haze or conversely higher optical clarity. Inherent differences in any “*in situ*” nucleators for a given resin could also influence superstructure size if such nucleators are operable at the time of crystallization. For the Ziegler-Natta blown film materials which in this report displayed relatively low total haze values, it was determined that their lower surface haze resulted from a smoother surface texture which was attributed to a lack of any distinct superstructure as was illustrated by AFM and SALS. Under certain processing conditions (e.g., very high shear rates or stresses), however, such that the polymer’s relaxation time scales distinctly exceed the process time scales (high Deborah number), high surface haze may

result even in the absence of any crystalline superstructure formation. It should be recognized that this high surface haze is attributed to melt rheological instabilities such as elasticity driven fine-scale surface roughness or even sharkskin melt fracture. In fact, we now have clear evidence, based on the study reported herein as well as related data obtained on other samples not discussed herein, that the total haze when plotted against the logarithm of the recoverable shear strain, γ_{∞} , yields a somewhat parabolic concave upward function. At low values of γ_{∞} , the superstructure we have discussed in this report is promoted which accents surface and hence total haze. As γ_{∞} increases, such superstructures are no longer developed but rather give rise to a more oriented stacked lamella-like texture thereby decreasing surface and hence total haze. However, at even higher γ_{∞} values representing highly melt elastic behavior, fine-scale surface roughness due to high melt elastic instabilities is induced, thereby again causing surface roughness to be

greatly enhanced and consequently increasing surface and total haze values. We expect to report more on this issue in our subsequent studies.

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